NON MALLEABLE ENCRYPTION APPARATUS AND METHOD

Claim for Priority

The present application is a continuation in part of parent application serial number 09/237,522 which was filed on January 27, 1999 and claims the priority of said parent application. The parent application was pending at the time of filing of the present continuation in part application.

Field of the Invention

This invention relates to improved methods and apparatus for encryption and decryption of data.

Background of the Invention

The present invention deals with the area of encryption and decryption of data messages. Encryption takes a cleartext message and produces an encrypted message also called a ciphertext. Decryption takes an encrypted message and produces its corresponding cleartext message.

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It is known in the prior art how to take a message and turn it into an encrypted message using a first user's public key. The first user upon receiving the encrypted message can then decrypt it, to reveal the original message, using the first user's secret key. The first user's public key is as the name implies, available to the public so that others can send messages to the first user. However, the first user's secret key is not available. The public key is associated with a one-way function, i.e. once the message is encrypted it cannot be decrypted without the secret key even though the public key and the encryption algorithms are known.

El Gamal encryption is a standard method of encryption known in the art. In this method a first processor performing the encryption step, takes a message m as an input; chooses a random value "c", and produces the outputs $a = m*y^c$ modulo p; $b = g^c$ modulo p. For El Gamal decryption, a second processor (which may be the first processor) calculates the data message m from $m = a/b^x$ modulo p. In the above $y = g^x$ modulo p is the public key and x is the secret key. The parameters g, x, and p and other system parameters are picked according to methods known to a person skilled in the art. The parameter g is a generator of the group G_p. If we take all possible values of x and compute g^x, this result will take all values in the group G_p which is a large set of values. The value c is chosen at random by the entity that performs the encryption.

The ElGamal encryption method has the following weaknesses:

(1)   Given an encryption (a,b) of an unknown data message m, it is possible to produce an encryption of a still unknown message, which corresponds to the value dm, by computing (a d modulo p, b). For example, if (a,b) is an encryption of the value m = 3, then (a',b') = (4a,b) is an encryption of the value 4m = 12. It is not necessary to know m to compute (a',b') from (a,b).

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(2)   Given the encryption pair or ciphertext (a,b) of data

message m, it is possible to produce a ciphertext of m^d as (a^d modulo p, b^d).

For example, a correct message could be raised to some exponent and

there would be no way of telling that that had occurred.

(3)   Given two ciphertexts (a1, b1) and (a2, b2), with (a1, b1)

being an encryption of m1 and (a2, b2) being an encryption of m2, it is

possible to produce a ciphertext of the product of m1*m2 modulo p as

(a1*a2 modulo p, b1*b2 modulo p).

These three disadvantages and other and related ones are referred to in literature as

malleability. Malleability is a threat to security, correctness of decryption of a message, and

privacy in many situations. For example in an auction scenario if an offer for a product by a first

individual is m, given the ciphertext a second individual can overbid and make his offer 2*m

without knowing how much "m" is but knowing that the second individual will win the bidding

process. Using a similar attack one can duplicate votes in an election to determine (later when all

votes are decrypted) what you voted (by looking for a duplicate). In the prior art malleability is

avoided by forcing the value of the data message m to be encrypted to be of a particular form,

such as to always end in a particular string of length approximately 100 bits. This technique of

avoiding malleability has two disadvantages:

(a)   First, it is not possible to determine that an encrypted message is of the

valid form without decrypting it.

(b)   Secondly, this is not known to result in a problem-free system (i.e. a 'non-

malleable encryption') and cannot be proved to result in a non-malleable

encryption.

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However, prior to the parent application there were no approaches better at dealing with the malleability problem without losing efficiency of the resulting scheme and ciphertext.

The parent application provides a non-malleable encryption method where an encryption technique and a signing technique are used. An encryption processor takes a data message and produces an encryption using an encryption process. The encryption may also be called a ciphertext and typically would be comprised of first and second ciphertext portions. A signing processor takes the encryption and adds a signature to the first and second ciphertext portions using, for example, the second ciphertext portion as the public key for the signature. A receiver processor receives the ciphertext and the signature, decrypts the ciphertext to form a first data message, and determines if the first data message is valid by verifying the signature.

The encryption processor of the parent application may employ ElGamal encryption for the encryption process to form the encryption. The signing processor may perform a Schnorr signature process for the signing process or any other similar discrete log based signature, as appreciated by those skilled in the art. The signing processor may use part of the encryption process to perform the signing process.

Summary of the Invention

The present invention provides an improvement over the parent application. The improvement is particularly useful for long data message lengths. The present invention also uses an encryption technique and a signing technique to provide a non-malleable encryption. An encryption processor takes a data message and produces an encryption using an encryption process. The result of the encryption may also be called a ciphertext. However, unlike the parent application, in an embodiment of the present invention, the ciphertext typically would be

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comprised of first, second, and third portions. This ciphertext could be of the form of: (a_{new}, b_{new},

E). A signing processor takes the encryption and adds a signature s_{new} to form a quadruplet of

first, second, third, and fourth portions in the form of: (a_{new}, b_{new}, s_{new}, E). A receiver processor

receives the quadruplet, decrypts the ciphertext to form a first data message, and determines if

the first data message is valid by verifying the signature.

The encryption processor may employ ElGamal encryption for the encryption process to

form the three portions of the ciphertext (a_{new}, b_{new}, E). The signing processor may perform a

Schnorr signature process for the signing process or any other similar discrete log based

signature, as appreciated by those skilled in the art. The signing processor may use part of the

encryption process to perform the signing process.

The above fast encryption method of is particularly useful for long message lengths. A

message m can be encrypted using a transmitter secret key z to form a quantity E. A

transmitter processor prepares a ciphertext quadruplet (a_{new}, b_{new}, s_{new}, E) where:

$$a_{new} = z^{*}\, y^{c} \text{ modulo } p \; ;$$

$$b_{new} = g^{c} \text{modulo } p \dot{;}$$

$$s_{new} = \text{signature }_{c}(a_{new}, b_{new}, E)$$

As in the parent application, $y = g^{x}$ modulo p is the public key and x is the receiver secret

key. The parameters g, x, and p according to methods known to a person skilled in the art and

the parameter g is a generator of the group G_{p}. The parameter c is a random number. The

transmitter processor sends the ciphertext quadruplet $(a_{new}, b_{new}, s_{new}, E)$ to a receiver

processor. The receiver processor verifies the signature on s_{new} using methods known in the

art. The receiver processor then decrypts a_{new} and b_{new} using the receiver secret key x to get

the transmitter secret key z, i.e. in the following manner: $z = a_{new}/b_{new}^{x}$. The receiver

processor uses the transmitter secret key k to decrypt E to get the message M.

Brief Description of the Drawings

Fig. 1 shows a diagram of an apparatus in accordance with a first embodiment of the

parent application;

Fig. 2 shows a flow chart of a method in accordance with an embodiment of the parent

application; and

Fig. 3 shows a diagram of a transmitter processor and a receiver processor in accordance

with an embodiment of the present invention; and

Fig. 4 shows a flow chart of a method in accordance with another embodiment of the

present invention.

Detailed Description of the Drawings

The embodiment of the parent application will be described with reference to Figs. 1 and

2. In the parent application in one embodiment an apparatus comprising an encryption processor

and a signing processor is provided. These processors may in fact be part of the same personal

computer. For some purposes the encryption processor and signing processor may need to be

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one and the same processor.   For example, there are two parts of the standard El Gamal

ciphertext, but these share the same value 'c', and so, the value "c" would be known by both the

encryption processor and the signing processor. In fact the encryption processor and the signing

processor may all need to be part of one and the same processor in some situations.   The

signature part may also use the value of c, and therefore, at least for the above example, needs to

be part of the same processor or party.

Fig. 1 shows an apparatus 10 comprised of an encryption processor 12 and a signing

processor 16. The signing processor is connected to a receiver processor 18. The processors 12

and 16 may actually be part of a single processor which may be a personal computer.   The

receiver processor 18 typically would be a separate personal computer but may also be part of the

same personal computer.

In the apparatus 10 the encryption processor 12 has an input port 12a. The encryption

processor 12 is also connected to the signing processor 16 via communications link 12b.

Communications link 12b, and the other communications links mentioned herein, may be any

apparatus for linking computers or circuitry such as a port connected to another port by a wire or a

fiber. The signing processor 16 is connected to the receiver processor 18 via communications link

16a. The receiver processor 18 has an output port 18a. The encryption processor 12 is also

connected to the signing processor 16 via port communications link 16b. It should be noted that

one or more or all of the encryption processor 12, signing processor 16, and receiver processor

18 may be implemented in a single processor through a single piece of computer software.

The operation of the apparatus 10 of Fig. 1 is as follows and is also shown in part in the

flow chart 100 of Fig. 2.   A plaintext message "m" is sent to the input port 12a of encryption

processor 12. The plaintext message may be a digital data message, which may be comprised of

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a plurality of digital data bits or signals. The message "m" is encrypted by the encryption processor 12 using a method such as ElGamal encryption or some other known encryption process. The encryption pair or encryption (a,b) is produced on communications link 12b and sent to the signing processor 16. The encryption process performed by the encryption processor 12 is shown in steps 102, 104, and 106 of Fig. 2. As shown in Fig. 2 for the input message "m", a random number "c" is first generated at step 102. The random number "c" is used to calculate the quantity $a = m*y^c$ modulo p and the quantity $b = g^c$ modulo p at the steps 104 and 106 in Fig. 2. The value "c" in this example would be in the range of $0 <= c <= q$; where q is the size of G_p.

The encryption pair (a,b) is sent to the signing processor 16. The random number c is also sent to the signing processor 16 from the encryption processor 12 via the communications link 16b At step 108 of Fig. 2, the signing processor 16 uses the random number 'c' which was chosen for the encryption process by encryption processor 12, to obtain a signature "s". The signing processor 16 may then execute step 110 of Fig. 2 by outputting the triplet (a,b,s) to the receiver processor 18.

The value for the signature "s" can be obtained for example by using the Schnorr signature scheme. For that scheme the following steps are followed:

(1)   a random value k is picked where $1 <= k <= q$;

(2) $r=g^k$ modulo p is computed;

(3) $\sigma = k - x\ h(M,r)$ mod q is computed;

where h () denotes a so-called hash function; and M = (a,b) is the message to be signed.

(4)   Output the signature (r, σ) which is what we call the signature "s";

The receiver processor 18 may use the input of (M, r, σ) in order to verify the signature and thus verify that the decrypted message is a decryption of a valid data message by verifying if

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$r=g^{\sigma}y^{h(m,r)}$ modulo p. The above signature generation and verification is well known to those skilled in the art.

The signature "s" is appended to the encryption pair (a, b) to form the triplet (a,b,s) and this is output on communications link 16a, as shown by step 110 in Fig. 2. This triplet is received at the receiver processor 18. The receiver processor 18 can then decrypt the encryption pair (a,b) to obtain the original message m by calculating $m = (a/b)^x$; where x is the secret decryption key of a user. The receiver processor 18 can also use the value "b" as a public key to determine if the triplet (a,b,s) is valid or not tampered with.

Encryption methods, other than ElGamal can be used, particularly variations of ElGamal. Signature methods other than Schnorr can be used such as Digital Signature Standard (hereinafter "DSS") which is a U.S. signature standard. Instead of a signature method, a proof-of-discrete-log system can be used. Several such methods are well known in the literature.

The Schnorr signature process uses one or both portions (a, b) of the standard ElGamal encryption as a public key, most likely just the portion 'b' of the standard ElGamal encryption and the corresponding secret portion (the random number 'c' above), to sign a message. A signature 's' is provided with the encrypted message. The signature 's' is a function of the encrypted message (a, b), potentially including publicly available information, such as the time or date. It can be publicly verified by anybody who gets the ciphertext but can only be generated by a party with knowledge of the secret random number "c" used for encryption used for encryption. In the example referred to, the signer's secret key is based on the random number "c" which is used by the entity or processor, such as encryption processor 12, which encrypts a message, such as message "m", and said encryption processor also preferably functions as a signing processor 16 which computes the ciphertext (a,b,s). The overall encryption data is now a triplet of (a,b,s). In

this case (a,b) or portions thereof act as the public key, (a,b) or a function thereof is the message

and "s" is the signature. The ciphertext (referring to (a,b, and s)) is said to be valid if "s" is the

signature on (a,b) with respect to the chosen public key (which is (a,b, or functions of these)).

This new encryption method can be proved to be non-malleable, i.e. given some number

of ciphertexts (a_i, b_i, s_i), it is impossible to produce a new or valid ciphertext from the old

ciphertexts, or a new and valid ciphertext with a plaintext message in any known way related to

the plaintext messages corresponding to the old ciphertexts. Furthermore, the validity of a

ciphertext can be publicly verified in an efficient manner using our proposed methods and

apparatus. It retains the property that given a ciphertext (a,b,s), and two potential plaintext

messages m1 and m2, it is impossible to determine which one corresponds to (a,b,s). The new

ciphertext (a,b,s) as opposed to the old (a,b), is decrypted as before, i.e. by calculating

$m = a/b^x$ modulo p after verifying that (a,b,s) is a valid ciphertext. The method described with

reference to Figs. 1 and 2 is for the parent application.

Fig. 3 shows a transmitter processor 200 and a receiver processor 202 employing a fast

encryption method in accordance with an embodiment of the present invention. The method is

shown in the flow chart 300 in Fig. 4.

In accordance with the method shown by Figs. 3 and 4, a new quantity, "z" is used. "z"

will be called the "transmitter secret key" and is thus a secret key only known to the transmitter

processor 200. At step 302 the transmitter processor 200 takes a message m and encrypts it

using the transmitter secret key z to form a quantity E.

At step 304 the transmitter processor 200 prepares a quadruplet $(a_{new}, b_{new}, s_{new}, \dot{E})$
where:

$$a_{new} = z^* y^c \text{ modulo p };$$
$$b_{new} = g^c \text{ modulo p};$$

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s_{new} = signature $_c(a_{new}, b_{new}, E)$;

E = encrypt$_z$ (m);

s_{new} = signature $_c(a_{new}, b_{new}, E)$ means that the entire quantity is signed.

As in the previous embodiments $y = g^x$ modulo p is the public key and x is the

receiver secret key.   The parameters g, x, and p are selected according to methods known to a

person skilled in the art and the parameter g is a generator of the group G_p. In this embodiment, c

is a random number and has a similar function as the random number "c" in the first embodiment.

These parameters may be selected in accordance with El Gamal encryption.

At step 306 the transmitter processor 200 sends the quadruplet (a_{new}, b_{new}, s_{new}, E) to

the receiver processor 202.

At step 308 the receiver processor 202 verifies the signature on s_{new} using methods

known in the art.

At step 310 the receiver processor 202 decrypts (a_{new}, b_{new}) using the receiver secret

key x to get the transmitter secret key z, i.e. in the following manner. $z = a_{new}/b_{new}^x$ modulo p.

At step 312 the receiver processor 202 uses the transmitter secret key z to decrypt E to

determine the message m.

The transmitter processor 200 and receiver processor 202 may be personal computers

which run computer software to implement the methods of the present invention and may be

connected by a communications link such as communications link 200a. The transmitter

processor 200 and receiver processor 202 may both have memory for storing intermediate or

final data messages, ciphertexts, quadruplets, or other computer data signals as needed.

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The last method is particularly advantageous for long data messages of many bits for

"m". This is because y^c can be thought of as a "blanket" which is used to hide what it is

multiplied by. Thus in the earlier embodiment y^c was multiplied by the message m. However,

in that case the message m could only be as many bits as y^c or the message m wouldn't be

hidden. Therefore in the earlier embodiment of the present invention, the message size of m

was limited to the size of y^c.

However, in the embodiment of Figs. 3 and 4, y^c was multiplied by z (the transmitter

secret key) and thus z would be limited in size (i.e. no. of bits) to the number of bits for y^c.

However, m would not be limited at all in size. The message "m" is made available to the

receiver processor by encrypting it using z to form E and transmitting E to the receiver

processor 202.

There may actually be a primary transmitter secret key z which can be chosen as, z =

g^γ modulo p, for a random value of γ chosen from the set [0..q]. The value q is chosen in

accordance with known encryption methods such as El Gamal encryption. If this primary

transmitter key z is not of the format used for producing the ciphertext E (e.g. is of the wrong

length) then a secondary temporary key z' can be computed as z' = f(z), where f is an abitrary

but agreed upon function, such as truncation. In the setting relating to triple – DES ("Digital

Encryption Standard"), for example, one would want the key z' used for encryption of m to form

E to be of the form z_1, z_2 such that z_1 and z_2 are both 56 bit keys. The quantities z_1 and z_2 can

be called portion keys. In this example, the function would truncate the primary transmitter key

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z to a length of 112 bits, and then divide the resulting secondary transmitter key z' into two

equal-sized portions z_1 and z_2, which can be done by letting z_1 be the first 56 bits of the

secondary transmitter key z' and z_2 the remaining 56 bits.

Instead of employing the mathematical operations (i.e. the exponentiation and multiplication shown)

$$a_{new} = z^* \, y^c \text{ modulo } p \; ;$$
$$b_{new} = g^c \text{modulo } p \; ;$$
$$s_{new} = \text{signature } _c(a_{new}, b_{new}, E)$$

mathematical operations may be employed using elliptical curves as known in the art.

The substitution of elliptical curve mathematical operations in cryptography is shown by "Use of

Elliptic Curves in Cryptography", copyright 1998, by Victor S. Miller, Exploratory Computer

Science, IBM Research, P.O. Box 218, Yorktown Heights, N.Y. 10598.; and "Non Supersingular

Elliptic Curves for Public Key Cryptosystems" by Beth, Schaefer, 1998 from the Institut for

Algorithmen and Kogntive Syteme Universitat Karksruhe, Fasanengarten 5, D-7500 Kariruhe 1.